

# Severe Accident Phenomenology short course



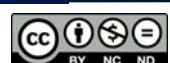
ETSII – Universidad Politécnica de Madrid  
19-23 June 2023

## Lecture 12b: Uncertainty Quantification in Severe Accident Analysis

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# The Complexity Domain



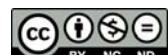
# Contents

- 1. The Title***
- 2. Background***
- 3. Methodology***
- 4. Present Challenges***
- 5. Main Takeaways***



# *Terms & Acronyms*

- **BEPU** *Best Estimate Plus Uncertainties*
- **UaSA** *Uncertainties and Sensitivity Analysis*
- **FoM** *Figure of Merit*
- **PDF** *Probability Density Function*



# The Source

- **BEPU was born within the domain of Thermal-hydraulics!**  
*Application of BE to ECCS licencing (USNRC: 1974-1986)*
- **In early 90's, OECD/CSNI WGs took over.**  
*(NEA/CSNI/R(1994)20; NEA/CSNI/R(97)35; NEA/CSNI R(97)4; ...)*  
**WGAMA:** - BEMUSE (2004-2010);  
- PREMIUM (2012-2015);  
- SAPIUM (2017-2019);  
- ATRIUM (2021-2024)

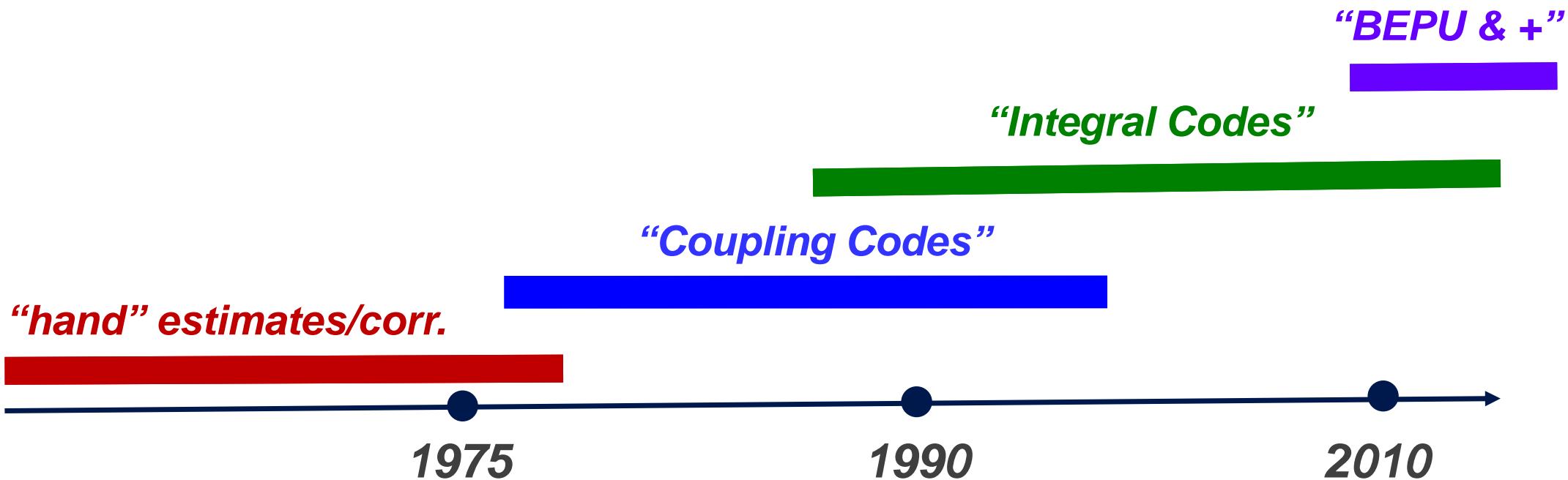


# *The Severe Accident Radiography*

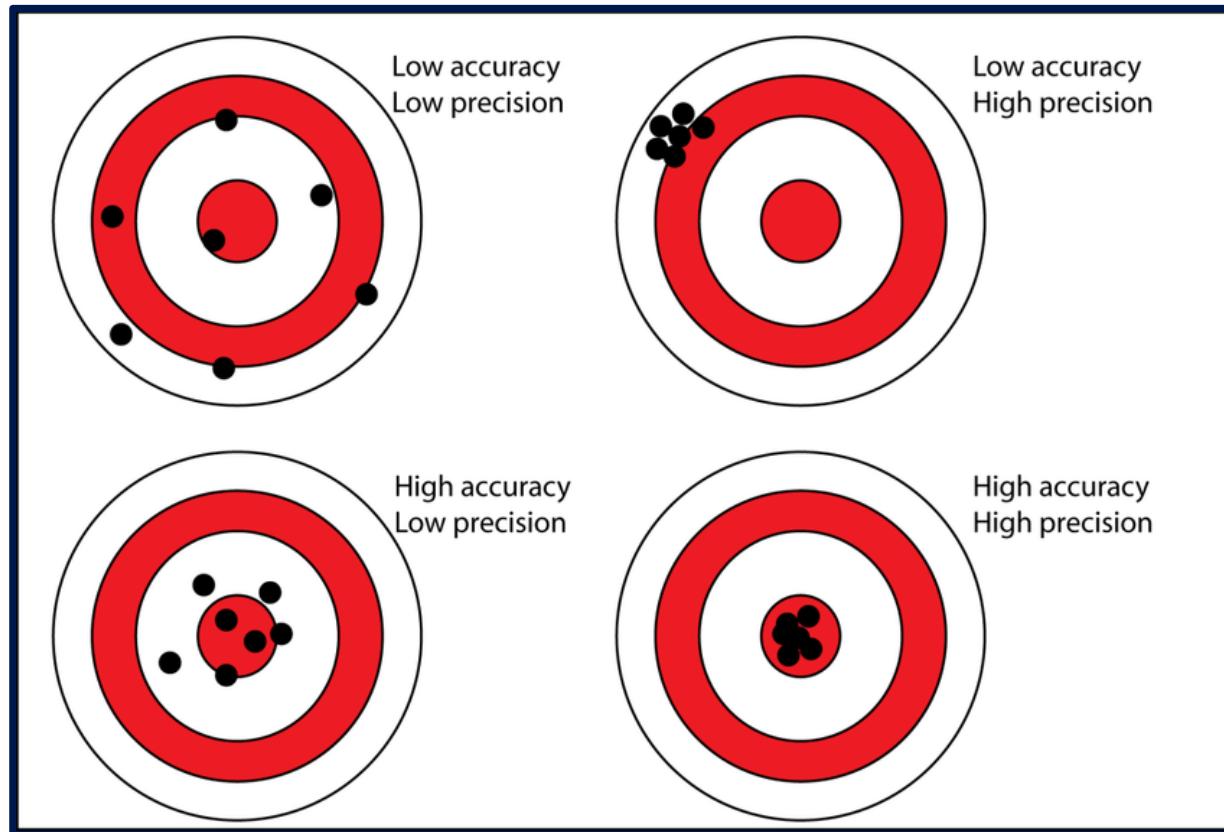
- **Phenomenological domain**
    - A huge number of phenomena.
    - Multidisciplinary (therm-fluid, mechanical, phys., chem, ...).
    - Strong feedback.
  - **Boundary conditions**
    - Broad ranges ( $T$ ,  $P$ ,  $D$ , ...).
    - Extreme values.
  - **Timing & Extension**
    - Integration over long periods (fast & slow phenomena).
    - Full NPP scope (micro & macro scale; safeguards; human action).



# The Time Perspective



# The Challenge



# The Opportunity

- “**Maturity**” of severe accident codes (*integration;phenomena;validation”;numerics*)
- **Computational resources presently available.**



## **Major advantages:**

- *Avoidance of conservative assumptions.*
- *Better identification of safety margins.*
- *Quantification of likelihood of reaching specific values.*
- *Insights into dominating uncertainties*

## **How accurate SA simulations are?**



# Severe Accident Codes

***Capitalization of knowledge on severe accidents***

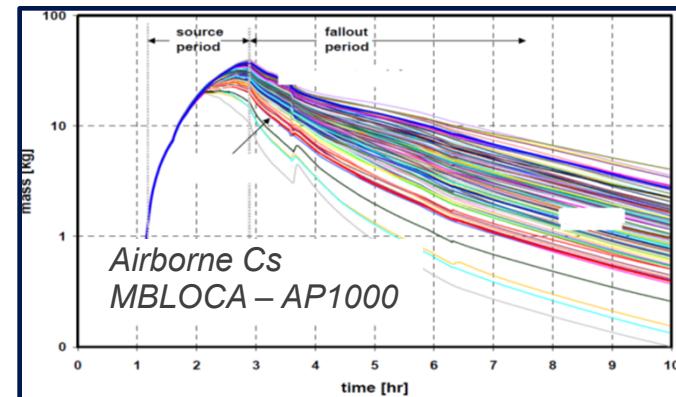
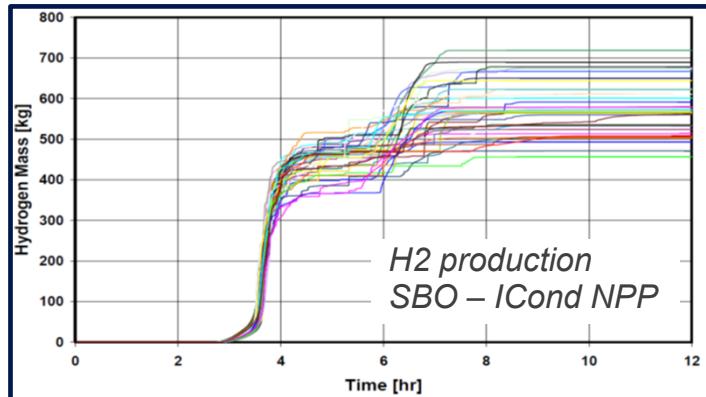
- ***Input build:*** Major hypo's & approximations
- ***Nature of models:*** “from empirical to pseudo-mechanistic”.
- ***Models integration*** →  $x_i, x_j, x_k, \dots (+ \Delta_i, \Delta_j, \Delta_k, \dots)$  transfer
- ***Variability of BC*** → nodalization
- ***Accident mgmt*** → timing?; efficiency?; equip. perform.

**Uncertainty  
Quantification  
(UQ)**



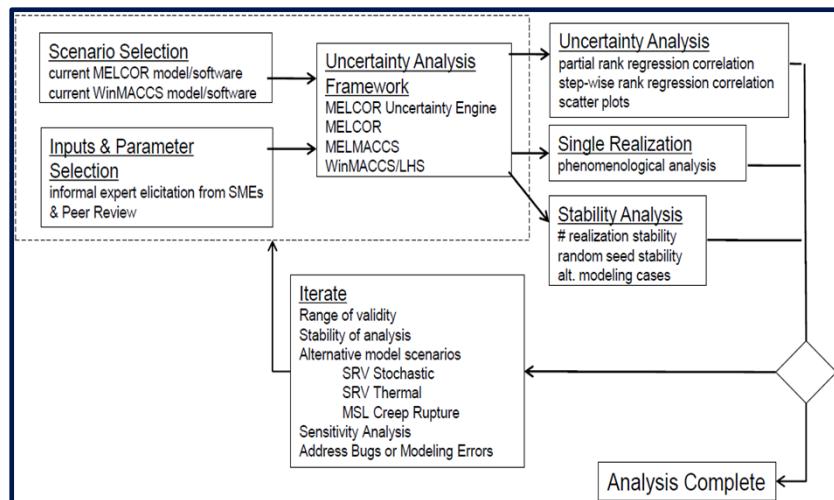
# BEPU in SA Analysis (I)

- A pioneer work based on STCP (Khatib-Rahbar et al., 1989)
  - Identification of input param.
  - Determination of pdf's
  - Random combination samp.
  - Calculation running
- Similar methodology based on MELCOR 1.8.5 (Gauntt R.O., 2005)

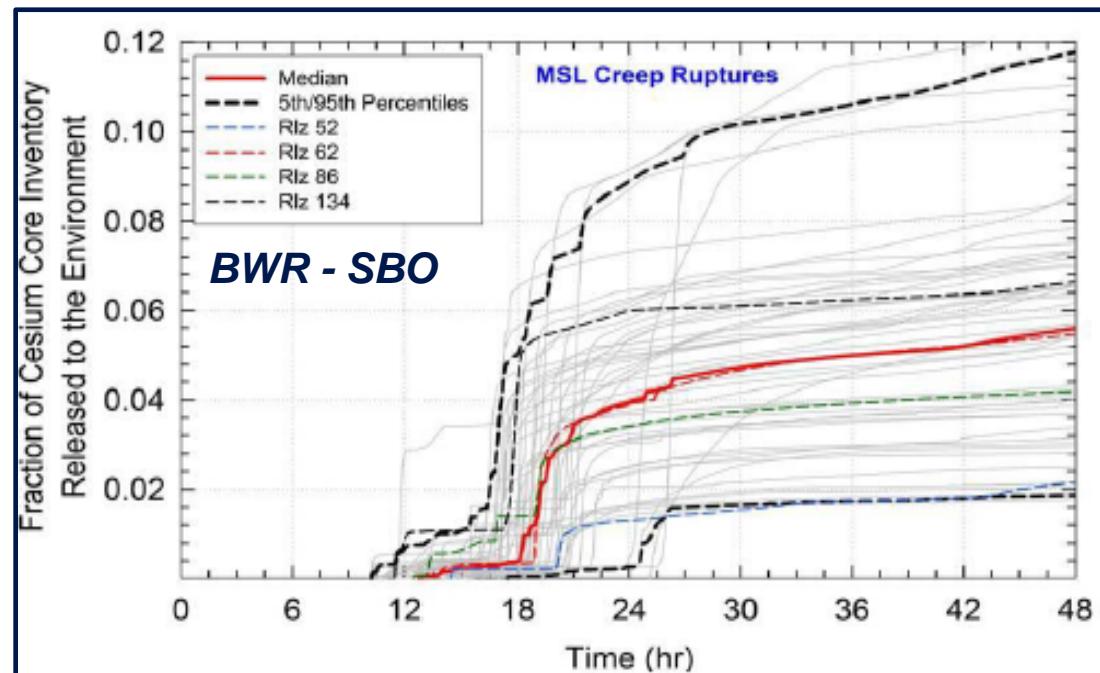


# BEPU in SA Analysis (II)

## *State of the Art Reactor Consequence Analyses (2017)*



- Battery duration; SRV failure rate; MSL creep rupture area; ...
- Zry breakout T; molten clad drainage drain; debris radial relocation; ...



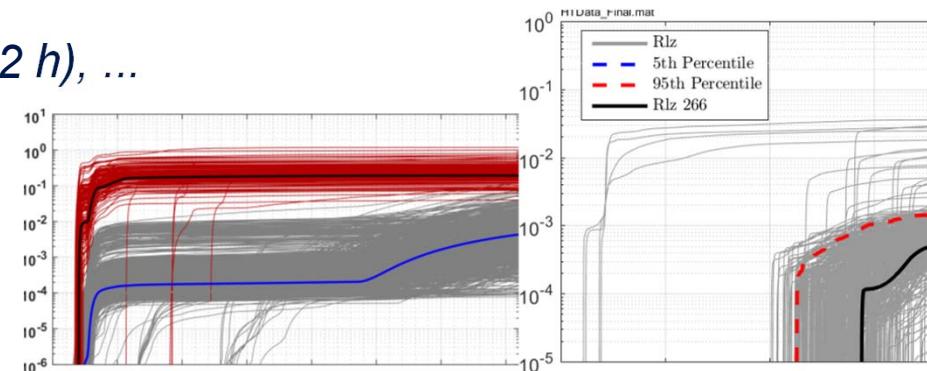
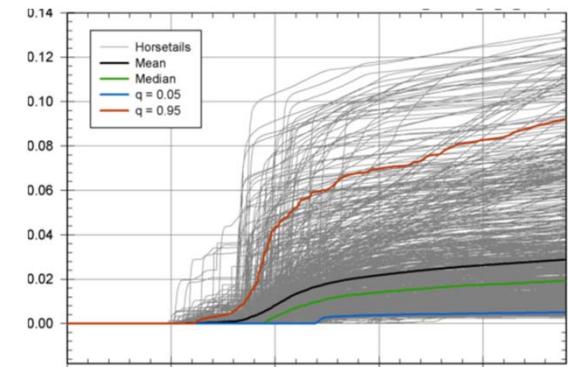
*A comprehensive list of uncertain parameters is practically unapproachable!*



# BEPU in SA Analysis (III)

**“Summary of the Uncertainty Analyses for the State-of-the-Art Reactor Consequence Analyses Project”**  
**(NUREG-2254; 2022)**

- 2010-2019.
- 3 “full-scope” UaSAs: PBottom; Surry; Sequoyah.
- Unmitigated LTSBO (PB), STSBOs (S&S).
- MELCOR-MAACS; MC (865, 567, 1147); LHS.
- Assumptions on SVs, breach (SGTR), time (48 h; 72 h), ...
- Expert judgement!!! (input parameters, 15-20).



# BEPU in SA Analysis (IV)

*The EU-MUSA Project*  
(2019-2023)

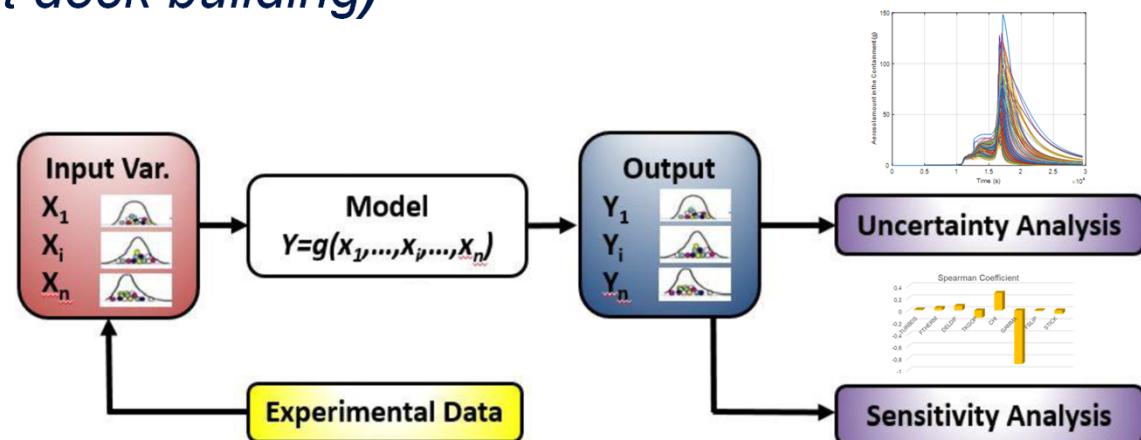


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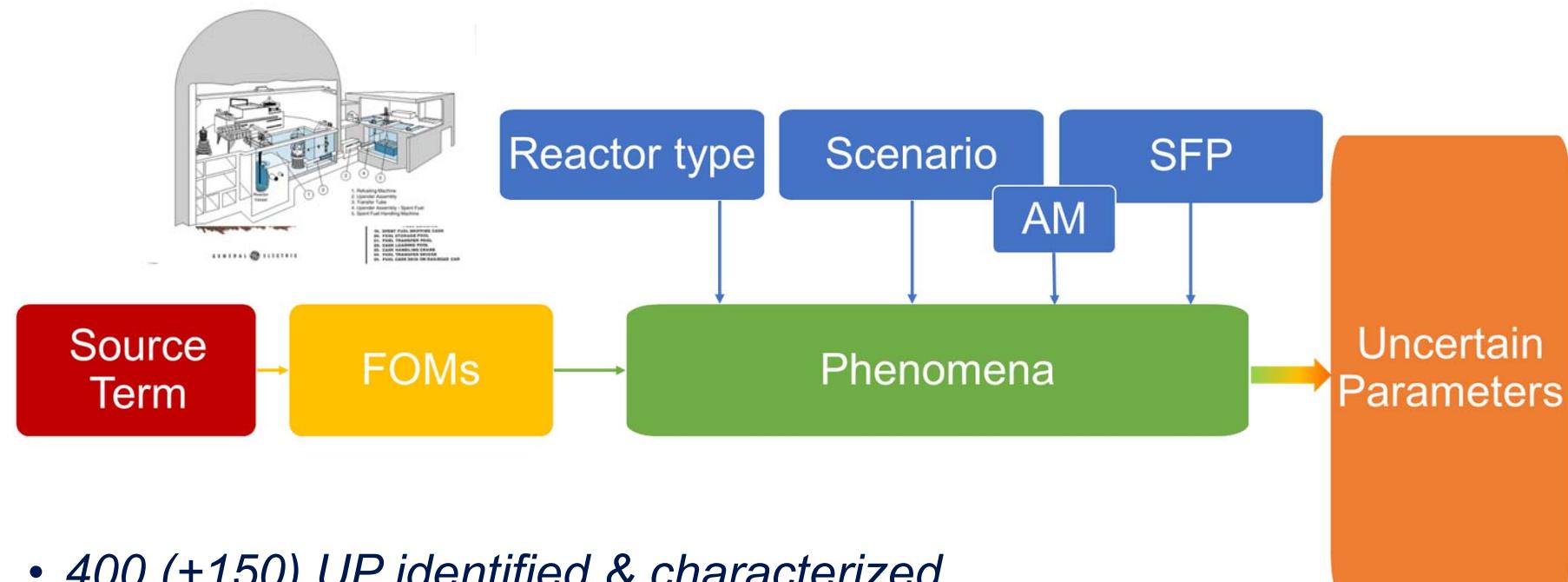


# Fundamental Steps

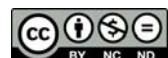
- Characterization of *Input parameters*
- *Generation of samples* (*input deck building*)
- *Propagation of samples*.
- *Evaluation of uncertainties*
- *Sensitivity Analysis*



# Characterization of Uncertain Parameters (The MUSA Project)

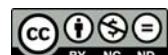


- 400 (+150) UP identified & characterized.
- Substantiated “expert judgement”.



# Characterization of Uncertain Parameters (The MUSA Project)

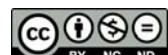
Phenomena	Uncertain Parameter	Reference value	Lower bound	Upper bound	pdf	References
<b>Sedimentation</b>	Gas viscosity [kg/ms]	1.0 / N/A	-5% / N/A	+5% / N/A	Uniform	Expert Judgment
	Gas temperature [K]	N/A	N/A	N/A	N/A	N/A
	Gas pressure [Pa]	1.55E+07 / N/A	-1.5% / N/A	+1.5% / N/A	Normal	Expert Judgment
	Gas mean free path	N/A	N/A	N/A	N/A	N/A
	Particle diameter Lower Bound [m]	0,00000011	0,00000001	0,0000002	Triangular	1986 Helton et al. "Uncertainty and Sensitivity Analysis of a Model for Multicomponent Aerosol Dynamics"; 2009 NEA/CSNI. "State-of-the-Art Report on Nuclear Aerosols"
	Particle diameter Upper Bound [m]	0,000199	0,000005	0,00002	Triangular	1986 Helton et al. "Uncertainty and Sensitivity Analysis of a Model for Multicomponent Aerosol Dynamics"; 2009 NEA/CSNI. "State-of-the-Art Report on Nuclear Aerosols"
	Slip factor (default = 1.257)	1,257	1,14	1,28	Triangular	1990 D. J. Rader. "Momentum slip correction factor for small particles in nine common gases"; MELCOR Default; Expert judgment (pdf)



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- **Reasonable**
- **Justifiable**
- **Defensible**



# ***Generation of Samples***

## ***(The MUSA Project)***

- ***Monte Carlo***  $(n \sim 10^3)$
- ***Wilks***  $(n \sim 10^2)$  *Order statistics*
- ***Sampling*** *SRS (random)*  
*LH (Latin Hypercube)*



# Propagation of Samples (The MUSA Project)

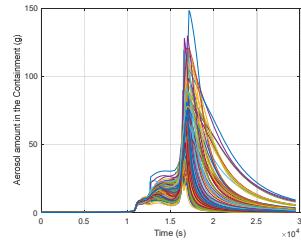


## Automatization!

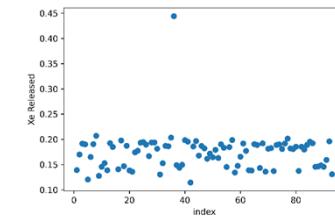


# Evaluation of Uncertainties (The MUSA Project)

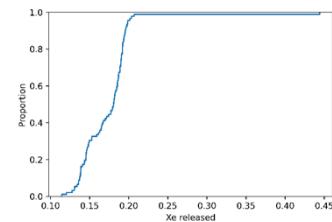
- *Dispersion plots*



- *Scatter plots*



- *CDF; PDF*



- *Descriptive statistics*

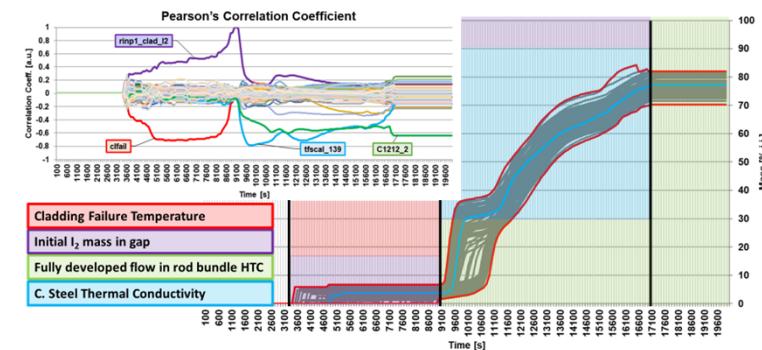
Statistical parameter	Xe
MELCOR reference case (% i.i.)	24.21
Mean (% i.i.)	17.33
Median (% i.i.)	18.07
Lower bound (% i.i.)	11.44
Upper bound (% i.i.)	44.42
Standard deviation (% i.i.)	3.71

...

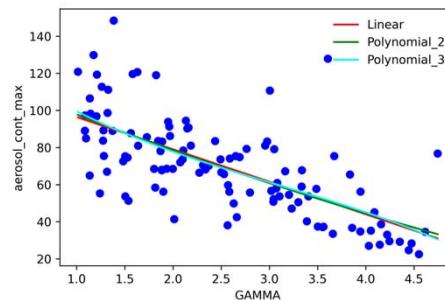


# Sensitivity Analysis (The MUSA Project)

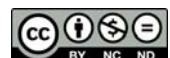
- **Correlation coefficients** (Pearson; Spearman)



- **Simple regressions**



- **More advanced techniques** (stepwise reg.; Lasso reg.)



# Present Challenges

- ***The UP database optimization*** (*filling; extension; restrc.*).
- ***A consolidation of UaSA application in SA*** (#UP; *nodding; FOMs; ...*)  
– ***Innovation.***
- ***A “balanced” use of expert judgement.***
- ***Further attention to accident management*** (*forward/reverse effect*).
- ***Show-cases for innovative technologies*** (*ST-ATFs; LW-SMR*)



- ***Uncertainties quantification of SA analysis is timely and necessary.***
- ***A systematic application of UASA in SA is far from straightforward.***
- ***Innovation needed to make UQ in SA a reality.***
- ***Cooperation of UQ application is the way (MUSA; IAEA/CRP).***
- ***New knowledge (statistics) brought and mastering needed.***
- ***Input deck characterization is fundamental.***
- ***Post-processing: Engineering judgement more necessary than ever.***



- Ross K., Phillips J., Gauntt R.O., Wagner K.C., 2014. *MELCOR Best Practices as Applied in the State-of-the-Art Reactor Consequence Analyses (SOARCA) Project*. NUREG/CR-7008.
- Ghosh S.T., Fuller E.L., Ross W., Gauntt R., 2017. *Insights from the Peach Bottom SOARCA Uncertainty Analysis*. IAEA Workshop on Advances in Understanding the Progression of Severe Accidents in Boiling Water Reactors.
- Nagase F., Gauntt R.O., Naito M., 2016. Overview and outcomes of benchmark study of the accident at the Fukushima Daiichi NPS (OECD/NEA BSAF Project). *Nuclear Technology* 196, 3, 499-510.
- Luxat D., Kalanich D., Hanophy J., Gauntt R., Wachowiak R., 2016. MAAP-MELCOR Crosswalk Phase 1 Study. *Nuclear Technology* 196, 3, 684-697.
- Khatib-Rahbar, M., et al., 1989. A Probabilistic Approach to Quantifying Uncertainties in the Progression of Severe Accidents. *Nuclear Science and Engineering* 102, 219-259.
- Gauntt, R.O, 2015. *Uncertainty Analyses Using the MELCOR Severe Accident Analysis Code*. OECD Workshop Proceeding, Aix-en-Provence, November 2005.





**Thank You!  
Any questions?**

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Wilks One-Sided	$\beta = 1 - \alpha^N$
Wilks Two-Side (Interval)	$\beta = 1 - \alpha^N - (N - 1)(1 - \alpha)\alpha^{N-1}$

Table 1: Minimum sample size required for  $(100 \times P)/(100(1 - \alpha))$  Wilks tolerance limits and bounds. Results are shown for four common predication/confidence combinations for ranks from 1 to 10.

$r$	95%/95%		95%/99%		99%/95%		99%/99%	
	Bound	Interval	Bound	Interval	Bound	Interval	Bound	Interval
1	59	93	90	130	299	473	459	662
2	93	153	130	198	473	773	662	1001
3	124	208	165	259	628	1049	838	1307
4	153	260	198	316	773	1312	1001	1596
5	181	311	229	371	913	1568	1157	1874
6	208	361	259	425	1049	1818	1307	2144
7	234	410	288	478	1182	2064	1453	2409
8	260	458	316	529	1312	2306	1596	2669
9	286	506	344	580	1441	2546	1736	2925
10	311	554	371	631	1568	2784	1874	3179

Porter, 2019. Wilks' formula applied to computational tools: A practical discussion and verification. Annals of Nuclear Energy.

